Introduction to Artificial Intelligence

Unit # 7

Acknowledgement

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Popular Machine Learning Techniques

- Classification
  - Classification Trees ✔
  - **Naïve Bayes**
  - Neural Networks
- Clustering
  - K-Means
  - Associative Memory

- In this course, the focus is on the classification techniques

Conditional Probability Example

	B		~B	
	C	~C	C	~C
A	12	5	9	2
~A	4	8	20	4

- P(A | B, C) = 12/16
- P(A, B | ~C) = 5 / 19
- P(B | ~A, C) = 4 / 24

Conditional Independence

- Two events A and B are independent if knowing that A has happened does not say anything about B happening.

$$P(A\ B) = P(A)\ P(B)$$
$$P(A \mid B) = P(A)$$

- Two events A and B are conditionally independent given a third event C precisely if the occurrence or non-occurrence of A and B are independent events in their conditional probability distribution given C.

$$P(A\ B \mid C) = P(A \mid C)\ P(B \mid C)$$
$$P(A \mid B\ C) = P(A \mid C)$$

Bayes Theorem

- $P(A \mid B) = \dfrac{P(B \mid A)\ P(A)}{P(B)}$

$$= \frac{P(B \mid A)\ P(A)}{P(B|A)P(A)+P(B|\neg A)P(\neg A)}$$

- P(A) is the prior probability and P(A | B) is the posterior probability.

- Suppose events $A_1, A_2, \ldots\ldots, A_k$ are mutually exclusive and exhaustive; i.e., exactly one of the events must occur. Then for any event B:

$$P(A_i \mid B) = \frac{P(B \mid A_i)\ P(A_i)}{\sum P(B \mid A_j)\ P(A_j)}$$

Example I

- According to American Lung Association, 7% of the population has lung cancer. Of these people having lung disease, 90% are smokers; and of those not having lung disease, 25.3% are smokers.
- Determine the probability that a randomly selected smoker has lung cancer.

Example I Solution

- Let L = Lung Cancer, S = Smoker
- Given that
  - P(L) = 0.07
  - P(S | L) = 0.90 P(~S | L) = 0.10
  - P(S | ~L) = 0.253 P(~S | ~L) = 0.747
- Find probability, P(L | S)

$$P(L \mid S) = \frac{P(S \cap L)}{P(S)} = \frac{P(S \mid L)P(L)}{P(S \mid L)P(L) + P(S \mid \sim L)P(\sim L)}$$

$$P(L \mid S) = \frac{0.9 \, x \, 0.07}{0.9 \, x \, 0.07 + 0.253 \, x \, 0.93}$$

Example II

- Assume that about 1 in 1000 individuals in a given organization have committed a security violation.
- Assume that the **sensitivity** of a routine screening polygraph is about 85%. That is, the probability that the polygraph report will indicate a concern is about 85% if the individual has committed a security violation.
- Assume the **specificity** of the polygraph is about 80%. That is, if the individual has not committed a security violation, there is about an 80% chance that the polygraph report will not indicate a concern.
- What is the posterior probability that an individual whose polygraph report indicates a concern has committed a security violation?

Example II Solution

- Let
  - S = Security Violation Committed,
  - T = Test Positive
- Given that
  - P(S) = 0.001
  - P(T | S) = 0.85 P(~T | S) = 0.15
  - P(T | ~S) = 0.20 P(~T | ~S) = 0.80
- Find probability, P(S | T)

$$P(S\,|T) = \frac{P(T\,|S)P(S)}{P(T\,|S)P(S) + P(T\,|{\sim}S)P({\sim}S)}$$

$$P(T|S) = \frac{0.85\ x\ 0.001}{0.85\ x\ 0.001 + 0.20\ x\ 0.999}$$

How to Estimate Probabilities from Data?

Tid	Refund	Marital Status	Taxable Income	Evade
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes

- Class: $P(C) = N_c/N$
  - e.g., P(No) = 7/10, P(Yes) = 3/10
- For discrete attributes:

$$P(A_i \mid C_k) = |A_{ik}| / N_c$$

  - where $|A_{ik}|$ is number of instances having attribute A_i and belongs to class C_k
  - Examples:

    P(Status=Married|No) = 4/7
    P(Refund=Yes|Yes)=0

Naïve Bayes
Classification: Mammals vs. Non-mammals

Name	Give Birth	Can Fly	Live in Water	Have Legs	Class
human	yes	no	no	yes	mammals
python	no	no	no	no	non-mammals
salmon	no	no	yes	no	non-mammals
whale	yes	no	yes	no	mammals
frog	no	no	sometimes	yes	non-mammals
komodo	no	no	no	yes	non-mammals
bat	yes	yes	no	yes	mammals
pigeon	no	yes	no	yes	non-mammals
cat	yes	no	no	yes	mammals
leopard shark	yes	no	yes	no	non-mammals
turtle	no	no	sometimes	yes	non-mammals
penguin	no	no	sometimes	yes	non-mammals
porcupine	yes	no	no	yes	mammals
eel	no	no	yes	no	non-mammals
salamander	no	no	sometimes	yes	non-mammals
gila monster	no	no	no	yes	non-mammals
platypus	no	no	no	yes	mammals
owl	no	yes	no	yes	non-mammals
dolphin	yes	no	yes	no	mammals
eagle	no	yes	no	yes	non-mammals

Give Birth	Can Fly	Live in Water	Have Legs	Class
yes	no	yes	no	?

- Train the model (learn the parameters) using the given data set.
- Apply the learned model on new cases.

Naïve Bayes

Classification: Mammals vs. Non-mammals

Name	Give Birth	Can Fly	Live in Water	Have Legs	Class
human	yes	no	no	yes	mammals
python	no	no	no	no	non-mammals
salmon	no	no	yes	no	non-mammals
whale	yes	no	yes	no	mammals
frog	no	no	sometimes	yes	non-mammals
komodo	no	no	no	yes	non-mammals
bat	yes	yes	no	yes	mammals
pigeon	no	yes	no	yes	non-mammals
cat	yes	no	no	yes	mammals
leopard shark	yes	no	yes	no	non-mammals
turtle	no	no	sometimes	yes	non-mammals
penguin	no	no	sometimes	yes	non-mammals
porcupine	yes	no	no	yes	mammals
eel	no	no	yes	no	non-mammals
salamander	no	no	sometimes	yes	non-mammals
gila monster	no	no	no	yes	non-mammals
platypus	no	no	no	yes	mammals
owl	no	yes	no	yes	non-mammals
dolphin	yes	no	yes	no	mammals
eagle	no	yes	no	yes	non-mammals

A: attributes

M: mammals

N: non-mammals

$$P(A|M) = \frac{6}{7} \times \frac{6}{7} \times \frac{2}{7} \times \frac{2}{7} = 0.06$$

$$P(A|N) = \frac{1}{13} \times \frac{10}{13} \times \frac{3}{13} \times \frac{4}{13} = 0.0042$$

$$P(A|M)P(M) = 0.06 \times \frac{7}{20} = 0.021$$

$$P(A|N)P(N) = 0.004 \times \frac{13}{20} = 0.0027$$

Give Birth	Can Fly	Live in Water	Have Legs	Class
yes	no	yes	no	?

P(A|M)P(M) > P(A|N)P(N)

=> Mammals

Example: Play Tennis

Outlook	Temperature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	P
rain	mild	high	false	P
rain	cool	normal	false	P
rain	cool	normal	true	N
overcast	cool	normal	true	P
sunny	mild	high	false	N
sunny	cool	normal	false	P
rain	mild	normal	false	P
sunny	mild	normal	true	P
overcast	mild	high	true	P
overcast	hot	normal	false	P
rain	mild	high	true	N

P(P) = 9/14

P(N) = 5/14

outlook	
P(sunny|p) = 2/9	P(sunny|n) = 3/5
P(overcast|p) = 4/9	P(overcast|n) = 0
P(rain|p) = 3/9	P(rain|n) = 2/5
temperature	
P(hot|p) = 2/9	P(hot|n) = 2/5
P(mild|p) = 4/9	P(mild|n) = 2/5
P(cool|p) = 3/9	P(cool|n) = 1/5
humidity	
P(high|p) = 3/9	P(high|n) = 4/5
P(normal|p) = 6/9	P(normal|n) = 2/5
windy	
P(true|p) = 3/9	P(true|n) = 3/5
P(false|p) = 6/9	P(false|n) = 2/5

Outlook	Temperature	Humidity	Windy	Class
rain	hot	high	false	?